



# KNOWLEDGE ORGANISER

NAME & FORM

YEAR 9  
AUTUMN TERM  
MATHS FOUNDATION



# Year 9 Foundation Knowledge Organiser

# Maths Knowledge Organiser

## THEORETICAL PROBABILITY



### Key Concepts

**Probabilities** can be described using **words** and **numerically**.

We can use **fractions**, **decimals** or **percentages** to represent a probability.

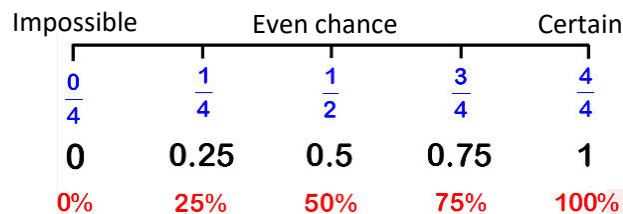
**Theoretical probability** is what should happen if all variables were fair.

All probabilities must **add to 1**.

The probability of something **NOT** happening equals:

$$1 - (\text{probability of it happening})$$

### Probability scale:



There are only red counters, blue counters, white counters and black counters in a bag.

Colour	Red	Blue	Black	White
No. of counters	9	3	5	2

- What is the probability that a blue counter is chosen?  $\frac{3}{19} = \frac{\text{number of blue}}{\text{total number of counters}}$
- What is the probability that red is **not** chosen?  $\frac{10}{19} = \frac{\text{number of all other colours}}{\text{total number of counters}}$

### Examples

There are only red counters, blue counters, white counters and black counters in a bag.

Colour	Red	Blue	Black	White
No. of counters	9	3x	x-5	2x

A counter is chosen at random, the probability it is red is  $\frac{9}{100}$ . Work out the probability is black.

$$\begin{aligned}
 9 + 3x + x - 5 + 2x &= 100 \\
 6x + 4 &= 100 \\
 x &= 16
 \end{aligned}$$

$$\begin{aligned}
 \text{Number of black counters} &= 16 - 5 \\
 &= 11
 \end{aligned}$$

$$\text{Probability of choosing black} = \frac{11}{100}$$

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### Key Words

Theoretical  
Probability  
Fraction  
Decimal  
Percentage  
Certain  
Impossible  
Even chance

	1	2	3
Prob	5	4	9

- Calculate the probability of choosing a 2.
- Calculate the probability of not choosing a 3.

	1	2	3
Prob	0.37	2x	x

- Calculate the probability of choosing a 2 or a 3.

ANSWERS: 1a)  $\frac{4}{18}$  b)  $\frac{18}{9}$  2)  $P(2) = 0.42$   $P(3) = 0.21$

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## RELATIVE FREQUENCY

### Key Concepts

**Experimental probability** differs to theoretical probability in that it is based upon the **outcomes from experiments**. It may not reflect the outcomes we expect.

Experimental probability is also known as the **relative frequency** of an event occurring.

**Estimating** the number of times an event will occur:

Probability  $\times$  no. of trials

### Examples

Colour	red	blue	white	black
Prob	$x$	0.2	0.3	$x$

A spinner is spun, it has four colours on it.

The relative frequencies of each colour are recorded.

The relative frequency of red and black are the same.

a) What is the relative frequency of red?

$$1 - (0.2 + 0.3) = 0.5$$

$$x = \frac{0.5}{2} = 0.25$$

b) If the spinner is spun 300 times, how many times do you expect it to land on white?

$$0.3 \times 300 = 90$$

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**Key Words**  
Experimental  
Relative  
frequency  
Fraction  
Decimal  
Probability  
Estimate

Number	1	2	3	4
Prob	$x$	0.46	0.28	$x$

A spinner is spun which has 1,2,3,4 on it. The probability that a 1 and a 4 are spun are equal.

a) What is the probability that a 4 is landed on?

b) If the spinner is spun 500 times how many times do we expect it to land on a 2?





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## LISTING OUTCOMES AND SAMPLE SPACE

### Key Concepts

When there are a number of different possible outcomes in a situation we need a **logical** and **systematic** way in which to view them all.

We can be asked to **list** all possible outcomes e.g. choices from a menu, order in which people finish a race.

We can also use a **sample space diagram**. This records the possible outcomes of two different events happening.

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**Key Words**  
List  
Outcome  
Sample  
space  
Probability

### Examples

Starter	Main
Fishcake Melon	Lasagne Beef Salmon

List all of the combinations possible when one starter and one main are chosen.

F, L    M, L  
F, B    M, B  
F, S    M, S

Note: You can write the initials of each option in a test. You do not need to write out the full word.

Two dice are thrown and the possible outcomes are shown in the sample space diagram below:

	1	2	3	4	5	6
1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(1,6)
2	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)	(2,6)
3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)
4	(4,1)	(4,2)	(4,3)	(4,4)	(4,5)	(4,6)
5	(5,1)	(5,2)	(5,3)	(5,4)	(5,5)	(5,6)
6	(6,1)	(6,2)	(6,3)	(6,4)	(6,5)	(6,6)

- 1) What is the probability that 2 numbers which are the same are rolled?

$$\frac{6}{36} = \frac{\text{outcomes where numbers are the same}}{\text{total number of outcomes}}$$

- 2) What is the probability that two even numbers are rolled?

$$\frac{9}{36} = \frac{\text{outcomes where numbers are both even}}{\text{total number of outcomes}}$$

- 1) Abe, Ben and Carl have a race. List all of the options for the order that the boys can end the race.

		Spinner		
Coin		Red	Green	Blue
	Heads	H,R	H,G	H,B
	Tails	T,R	T,G	T,B

- 2a) What is the probability that a head is landed on?  
b) What is the probability that a head and a green are landed on?

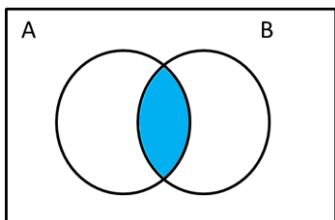
ANSWERS: 1) ABC, ACB, BAC, BCA, CAB, CBA 2a)  $\frac{1}{2}$  b)  $\frac{1}{6}$

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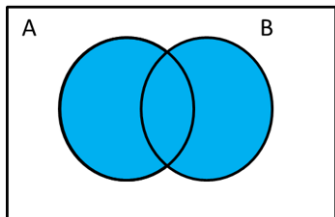
## FURTHER PROBABILITY



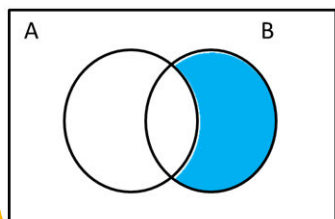
### Key Concept



$$P(A \cap B)$$



$$P(A \cup B)$$



$$P(A' \cap B)$$

### Key Words

**Probability:** The chance of something happening as a numerical value.

**Impossible:** The outcome cannot happen.

**Certain:** The outcome will definitely happen.

**Even chance:** There are two different outcomes each with the same chance of happening.

**Mutually Exclusive:** Two events that cannot both occur at the same time.

### Formula

$$P(A \cap B) = P(A) \times P(B)$$

$$P(A \cup B) = P(A) + P(B)$$

$$\text{or (non ME)} \quad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

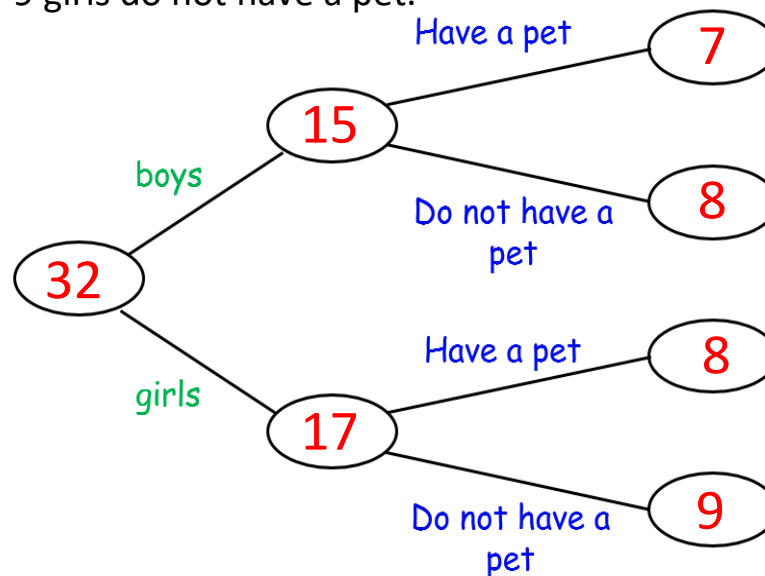
### Examples

In Hannah's class there are 32 students.

15 of these students are boys.

7 of the boys have a pet.

9 girls do not have a pet.



$$P(\text{boy}) = \frac{15}{32}$$

$$P(\text{Girl with pet}) = \frac{8}{32}$$

### Questions

- 1) Draw a two-way table for the question above.
- 2) Find the probability that a pupil chosen is a boy with no pets.
- 3) A girl is chosen, what is the probability she has a pet?

ANSWERS:

$$2) \frac{32}{8}$$

$$3) \frac{17}{8}$$

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## ORDER OF OPERATIONS

### Key Concept

- B** Brackets
- I** Indices
- D** Division
- M** Multiplication
- A** Addition
- S** Subtraction

If a calculation contains the looped calculations work from left to right.

### Key Words

**Operation:** In maths these are the functions  $\times \div + -$ .

**Commutative:** Calculations are commutative if changing the order does not change the result.

**Associative:** In these calculations you can re-group numbers and you will get the same answer.

**Indices:** These are the squares, cubes and powers.

### Tip

- Put brackets around the calculations which need to be done first.
- Indices also includes roots.

### Examples

$$\underbrace{5 \times 4}_{20} - \underbrace{8 \div 2}_4 = 16$$

$$\begin{aligned} & (2^2 + 6)^2 \times 4 - 8 \\ & \downarrow \\ & (4 + 6)^2 \times 4 - 8 \\ & \downarrow \\ & (10)^2 \times 4 - 8 \\ & \downarrow \\ & 100 \times 4 - 8 \\ & \downarrow \\ & 400 - 8 = 392 \end{aligned}$$

### Questions

- 1)  $7 - 10 \div 2$
- 2)  $4^3 - 13 \times 4$
- 3)  $21 \div 7 - 2$
- 4)  $12 \div (7 - 3)$
- 5)  $20 \div 2^2$
- 6)  $(16 - 13) \div 3$
- 7) Place brackets to make the calculation work  $20 \div 5 - 3 = 10$

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$$\frac{46.2 - 9.85}{\sqrt{16.3 + 5.42}}$$

$$\frac{50 - 10}{\sqrt{20 + 5}}$$

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## CALCULATIONS, CHECKING AND ROUNDING

### Key Concepts

A value of 5 to 9 rounds the number up.

A value of 0 to 4 keeps the number the same.

Estimation is a result of rounding to one significant figure.

### Examples

**Round 3.527 to:**

a) 1 decimal place

$$3.5\overset{\cdot}{2}7 \rightarrow 3.5$$

b) 2 decimal places

$$3.52\overset{\cdot}{7} \rightarrow 3.53$$

c) 1 significant figure

$$3.\overset{\cdot}{5}27 \rightarrow 4$$

**Estimate** the answer to the following calculation:

$$\frac{46.2 - 9.85}{\sqrt{16.3 + 5.42}}$$

$$\frac{50 - 10}{\sqrt{20 + 5}}$$

$$\frac{40}{5} = 8$$

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### Key Words

Integers  
Operation  
Negative  
Significant figures  
Estimate

- A) Round the following numbers to the given degree of accuracy  
 1) 14.1732 (1 d.p.) 2) 0.0568 (2 d.p.) 3) 3418 (1 S.F.)  
 B) Estimate:  
 1)  $\sqrt{4.09 \times 8.96}$  2)  $25.76 - \sqrt{4.09 \times 8.96}$   
 3)  $\sqrt[3]{26.64} + \sqrt{80.7}$  4)  $\frac{\sqrt{6.91 \times 9.23}}{3.95^2 \div 2.02^3}$





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## INDICES AND ROOTS



### Key Concepts

$$a^m \times a^n = a^{m+n}$$

$$a^m \div a^n = a^{m-n}$$

$$(a^m)^n = a^{mn}$$

$$a^{\frac{1}{n}} = \sqrt[n]{a}$$

$$a^{-m} = \frac{1}{a^m}$$

### Examples

**Simplify** each of the following:

$$1) a^6 \times a^4 = a^{6+4} \\ = a^{10}$$

$$2) a^6 \div a^4 = a^{6-4} \\ = a^2$$

$$3) (a^6)^4 = a^{6 \times 4} \\ = a^{24}$$

$$4) (3a^4)^3 = 3^3 a^{4 \times 3} \\ = 27a^{12}$$

$$5) \frac{5^2 \times 5^6}{5^4} = \frac{5^8}{5^4} \\ = 5^{8-4} \\ = 5^4$$

$$6) a^{\frac{1}{2}} = \sqrt{a}$$

$$7) 9^{\frac{1}{2}} = \sqrt{9} \\ = 3 \text{ or } -3$$

$$8) 2^{-3} = \frac{1}{2^3} = \frac{1}{8}$$

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### Key Words

Powers

Roots

Indices

Reciprocal

**Simplify:**

$$1) a^3 \times a^2 \quad 2) b^4 \times b \quad 3) d^{-5} \times d^{-1} \quad 4) m^6 \div m^2 \quad 5) n^4 \div n^4$$

$$6) \frac{8^4 \times 8^5}{8^6} \quad 7) \frac{4^9 \times 4}{4^3} \quad 8) (3^2)^5 \quad 9) 81^{\frac{1}{2}} \quad 10) 5^{-2}$$

ANSWERS: 1)  $a^5$  2)  $b^5$  3)  $d^{-6}$  4)  $m^4$  5) 1 6)  $8^3$  7)  $4^7$  8)  $3^{10}$  9) 9 or -9 10)  $\frac{1}{25}$



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## STANDARD FORM



### Key Concepts

We use standard form to write a very large or a very small number in scientific form.

Must be  $\times 10^b$   
 $b$  is an integer

$$a \times 10^b$$

Must be  $1 \leq a < 10$

### Examples

Write the following in **standard form**:

1)  $3000 = 3 \times 10^3$

2)  $4580000 = 4.58 \times 10^6$

3)  $0.0006 = 6 \times 10^{-4}$

4)  $0.00845 = 8.45 \times 10^{-3}$

Calculate the following, write your answer in **standard form**:

1)  $(3 \times 10^3) \times (5 \times 10^2)$

$$\left. \begin{array}{l} 3 \times 5 = 15 \\ 10^3 \times 10^2 = 10^5 \end{array} \right\} \begin{array}{l} 15 \times 10^5 \\ = 1.5 \times 10^6 \end{array}$$

2)  $(8 \times 10^7) \div (16 \times 10^3)$

$$\left. \begin{array}{l} 8 \div 16 = 0.5 \\ 10^7 \div 10^3 = 10^4 \end{array} \right\} \begin{array}{l} 0.5 \times 10^4 \\ = 5 \times 10^3 \end{array}$$

A) Write the following in standard form:

1) 74 000    2) 1 042 000    3) 0.009    4) 0.000 001 24

B) Work out:

1)  $(5 \times 10^2) \times (2 \times 10^5)$     2)  $(4 \times 10^3) \times (3 \times 10^8)$

3)  $(8 \times 10^6) \div (2 \times 10^5)$     4)  $(4.8 \times 10^2) \div (3 \times 10^4)$

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### Key Words

Standard form  
Base 10

### Links

Science

ANSWERS: A1)  $7.4 \times 10^4$  2)  $1.042 \times 10^6$  3)  $9 \times 10^{-3}$  4)  $1.24 \times 10^{-6}$   
B1)  $1 \times 10^8$  2)  $1.2 \times 10^{12}$  3)  $4 \times 10^4$  4)  $1.6 \times 10^{-2}$



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## EXPRESSIONS/EQUATIONS/IDENTITIES AND SUBSTITUTION



### Key Concepts

A **formula** involves two or more letters, where one letter equals an **expression** of other letters.

An **expression** is a sentence in algebra that does NOT have an equals sign.

An **identity** is where one side is the equivalent to the other side.

When **substituting** a number into an expression, replace the letter with the given value.

### Examples

- 1)  $5(y + 6) \equiv 5y + 30$  is an **identity** as when the brackets are expanded we get the answer on the right hand side
- 2)  $5m - 7$  is an **expression** since there is no equals sign
- 3)  $3x - 6 = 12$  is an **equation** as it can be solved to give a solution
- 4)  $C = \frac{5(F - 32)}{9}$  is a **formula** (involves more than one letter and includes an equal sign)
- 5) Find the value of  $3x + 2$  when  $x = 5$   
 $(3 \times 5) + 2 = 17$
- 6) Where  $A = b^2 + c$ , find A when  $b = 2$  and  $c = 3$   
 $A = 2^2 + 3$   
 $A = 4 + 3$   
 $A = 7$

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### Key Words

Substitute  
Equation  
Formula  
Identity  
Expression

### Questions

- 1) Identify the equation, expression, identity, formula from the list  
(a)  $v = u + at$  (b)  $u^2 - 2as$   
(c)  $4x(x - 2) = x^2 - 8x$  (d)  $5b - 2 = 13$
- 2) Find the value of  $5x - 7$  when  $x = 3$
- 3) Where  $A = d^2 + e$ , find A when  $d = 5$  and  $e = 2$

(d) equation

(c) identity

(b) expression

ANSWERS: 1) (a) formula  
3)  $A = 27$   
2) 8

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## EQUATIONS IN CONTEXT



### Key Concepts

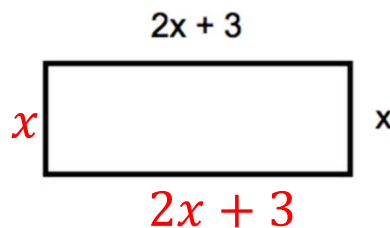
Algebra can be used to support us to find unknowns in a **contextual problem**.

We can always apply a letter to an unknown quantity, to then **set up an equation**.

It will often be used in area and perimeter problems and angle problems in geometry.

Solve to find the value of  $x$  when the perimeter is 42cm.

**HINT:** Write on all of the lengths of the sides.



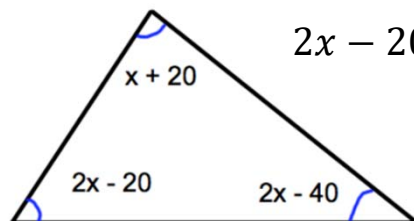
$$2x + 3 + 2x + 3 + x + x = 42$$

$$9x + 6 = 42$$

$$6x = 36$$

$$x = 6$$

We know the perimeter is 42cm



$$2x - 20 + x + 20 + 2x - 40 = 180$$

$$5x - 40 = 180$$

$$5x = 220$$

$$x = 45$$

Angles in a triangle sum to 180°

### Examples

Jane is 4 years older than Tom.  
David is twice as old as Jane.  
The sum of their ages is 60.  
Using algebra, find the age of each person.

$$\text{Tom} = x \longrightarrow 12$$

$$\text{Jane} = x + 4 \longrightarrow 12 + 4 = 16$$

$$\text{David} = 2x + 8 \longrightarrow (2 \times 12) + 8 = 32$$

$$x + x + 4 + 2x + 8 = 60$$

$$4x + 12 = 60$$

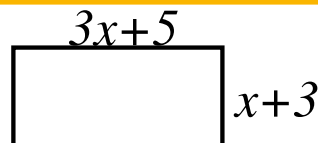
$$4x = 48$$

$$x = 12$$

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### Key Words

Solve  
Term  
Inverse  
operation



1) If the perimeter is 40cm. What is the length of the longest side?

2) Jane is 12 years older than Jack.  
Sarah is 3 years younger than Jack.  
The sum of their ages is 36.  
Using algebra, find the age of each person.

ANSWERS: 1)  $x = 3$  therefore the longest length is 14cm 2) Jack = 9, Jane = 21, Sarah = 6





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## REARRANGE AND SOLVE EQUATIONS

### Key Concepts

#### Solving equations:

Working with inverse operations to find the value of a variable.

#### Rearranging an equation:

Working with inverse operations to isolate a highlighted variable.

In solving and rearranging we **undo the operations** starting from the last one.

For each step in solving an equation we must do the **inverse** operation

Solve:

$$\begin{array}{l} 12 = 3x - 18 \\ +18 \qquad +18 \\ 30 = 3x \\ \div 3 \qquad \div 3 \\ x = 10 \end{array}$$

Solve:

$$\begin{array}{l} 5(x - 3) = 20 \\ \text{Expand} \\ 5x - 15 = 20 \\ +15 \qquad +15 \\ 5x = 35 \\ \div 5 \qquad \div 5 \\ x = 7 \end{array}$$

Solve:

$$\begin{array}{l} 7p - 5 = 3p + 3 \\ -3p \qquad -3p \\ 4p - 5 = 3 \\ +5 \qquad +5 \\ 4p = 8 \\ \div 2 \qquad \div 2 \\ p = 2 \end{array}$$

### Examples

**Rearrange** to make  $r$  the subject of the formulae :

$$\begin{array}{l} Q = \frac{2r - 7}{3} \\ \times 3 \qquad \times 3 \\ 3Q = 2r - 7 \\ +7 \qquad +7 \\ 3Q + 7 = 2r \\ \div 2 \qquad \div 2 \\ \frac{3Q + 7}{2} = r \end{array}$$

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### Key Words

Solve  
Rearrange  
Term  
Inverse  
operation

- 1) Solve  $7(x + 2) = 35$
- 2) Solve  $4x - 12 = 28$
- 3) Solve  $4x - 12 = 2x + 20$

4) Rearrange to make  $x$  the subject:

$$y = \frac{3x + 4}{2}$$

ANSWERS: 1)  $x = 3$  2)  $x = 10$  3)  $x = 16$  4)  $x = \frac{2y - 4}{3}$



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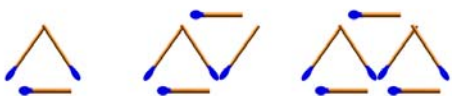
## SEQUENCES



### Key Concept

#### Types of Sequence

Sequence as pictures:



Linear sequence:

4, 7, 10, 13, 16, ...



Fibonacci sequence:

(add the previous two terms)

1, 1, 2, 3, 5, 8, ...

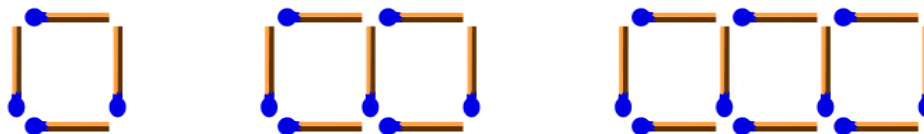
### Key Words

**Sequence:** A list which is in a particular order following a pattern.

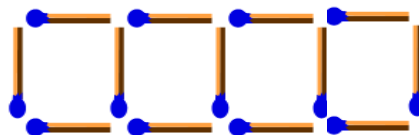
**Term:** Each particular part of a sequence.

**Linear sequence:** A sequence which is formed by adding or subtracting the same amount each time.

### Examples



Next pattern is:



Sequence = 4, 7, 10, 13, ...

Term to term rule = + 3

Nth term

4, 7, 10, 13, 16, ... =  $3n + 1$

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### Tip

If a sequence is decreasing, the 'n' term will be negative.

Eg, 15, 11, 7, 3, ...

Nth term =  $-4n + 19$

### Questions

1) Find the next two terms and the term to term rule

a) 9, 13, 17, 21, ...   b) 7, 12, 17, 22, ...   c) 9, 7, 5, 3, ...   d) 3, 4, 7, 11, 18

2) Find the nth term   a) 7, 9, 11, 13, ...   b) 8, 13, 18, 23, ...

c) 15, 12, 9, 6, ...   d) 1, -3, -7, -11, ...

ANSWERS: 1) a) 25, 29 Rule = +4   b) 27, 32, Rule = +5   c) 1, -1, Rule = -2   d) 29, 47, Rule = add previous 2 numbers   2) a)  $2n + 5$    b)  $5n + 3$    c)  $-3n + 18$    d)  $-4n + 5$

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## SEQUENCES



### Key Concepts

#### Arithmetic or linear sequences

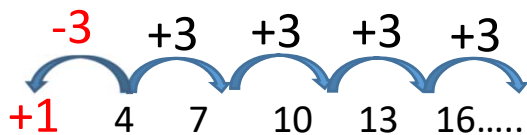
increase or decrease by a common amount each time.

**Geometric series** has a common multiple between each term.

**Quadratic sequences** include an  $n^2$ . It has a common second difference.

**Fibonacci sequences** are where you add the two previous terms to find the next term.

### Linear/arithmetic sequence:



a) State the  $n$ th term

$$3n + 1$$

Difference      The 0<sup>th</sup> term

b) What is the 100<sup>th</sup> term in the sequence?

$$3n + 1$$

$$3 \times 100 + 1 = 301$$

c) Is 100 in this sequence?

$$3n + 1 = 100$$

$$3n = 99$$

$$n = 33$$

Yes as 33 is an integer.

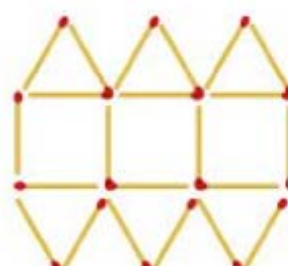
Pattern 1



Pattern 2



Pattern 3



**Hint:** Firstly write down the number of matchsticks in each image:

$$7n + 1$$

Pattern 1	Pattern 2	Pattern 3
8	15	22

+1

-7      +7      +7

**Geometric sequence e.g.**

$$\times 3$$

$$4 \quad 12 \quad 36 \quad 108...$$

**Quadratic sequence e.g.**

$n^2 + 4$  Find the first 3 numbers in the sequence

First term:  $1^2 + 4 = 5$

Third term:  $3^2 + 4 = 13$

Second term:  $2^2 + 4 = 8$

### Key Words

Linear  
Arithmetic  
Geometric  
Sequence  
Nth term

1) 1, 8, 15, 22, ...

a) Find the  $n$ th term    b) Calculate the 50<sup>th</sup> term    c) Is 120 in the sequence?

2)  $n^2 - 5$  Find the first 4 terms in this sequence

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## DISTANCE-TIME GRAPHS



### Key Concepts

A **distance-time** graph, plots time against the distance away from a starting point.

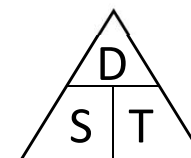
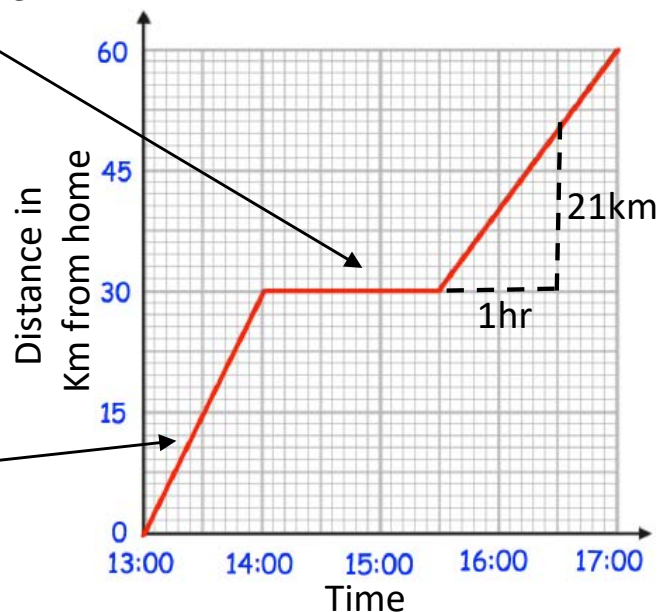
**Speed** can be calculated from these graphs by finding the gradient of the graph.

Horizontal lines are sections where the object is stationary.

### Examples

Horizontal sections are where the object is stationary

Diagonal lines show the object moving away from home or moving closer to home



$$\text{Speed} = \frac{\text{distance}}{\text{time}}$$

$$\text{Speed} = \frac{21}{1}$$

$$\text{Speed} = 21\text{km/h}$$

### Key Words

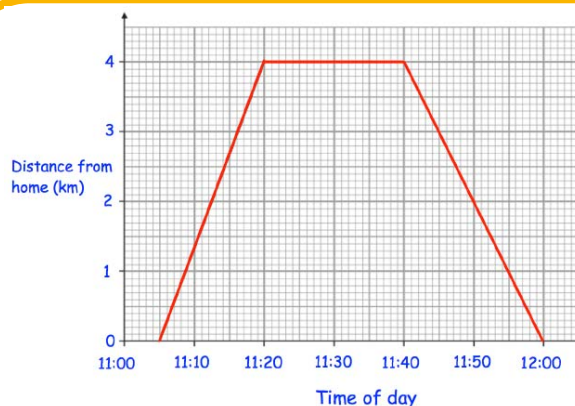
**Distance**

**Time**

**Speed**

**Gradient**

**Stationary**



A distance-time graph shows the journey of someone from home to the shop and back again.

- 1) How long were they at the shop for?
- 2) How far away from home is the shop?
- 3) How far did they travel in total?
- 4) What speed did they travel on the way to the shop in km/h?

**Y9**

**Foundation**





# Maths Knowledge Organiser

## STRAIGHT LINE GRAPHS AND EQUATION OF A



### Key Concepts

**Coordinates** in 2D are written as follows:

$x$  is the value that is to the left/right  
 $y$  is the value that is to up/down

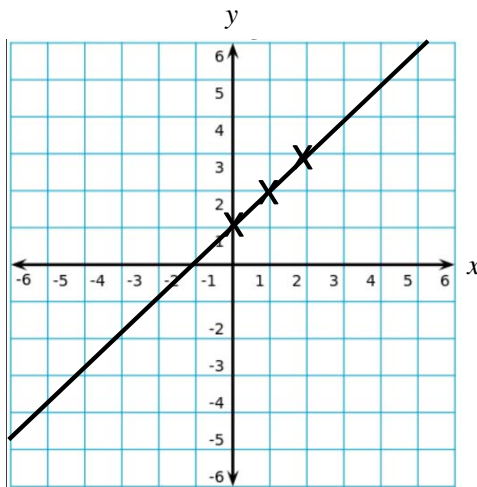
**Straight line graphs** always have the equation:

$$y = mx + c$$

$m$  is the **gradient** i.e. the steepness of the graph.  
 $c$  is the **y intercept** i.e. where the graph cuts the y axis.

Plot the graph of  $y = x + 1$

$x$	0	1	2
$y$	1	2	3



### Examples

Calculate the equation of this line:

$$y = mx + c$$

$$m = \frac{4}{2} = 2$$

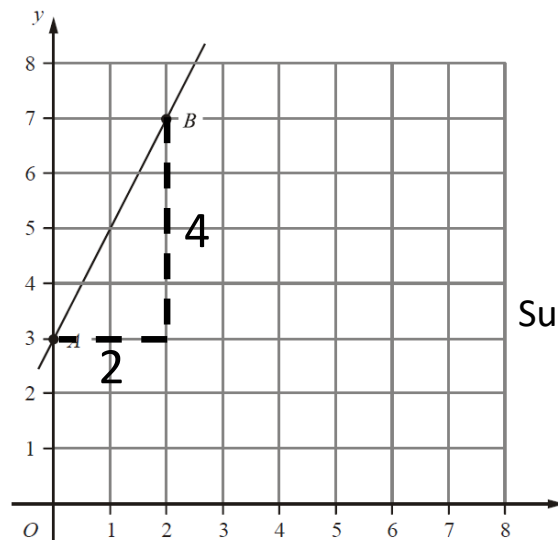
$$y = 2x + c$$

Substitute in a coordinate: (2,7)

$$7 = (2 \times 2) + c$$

$$3 = c$$

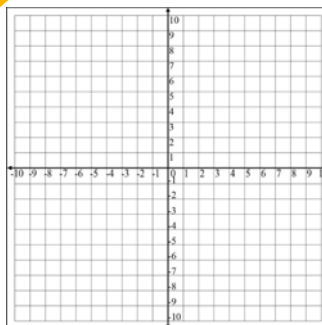
$$y = 2x + 3$$



Y9

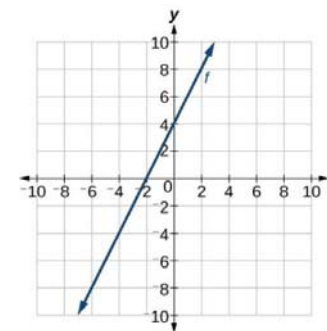
Foundation

**Key Words**  
**Coordinate**  
**Gradient**



1) Plot the line  $y = 3x - 2$

2) Find the equation of the line for the attached graph.



ANSWERS: 2)  $y = 2x + 4$



# Maths Knowledge Organiser

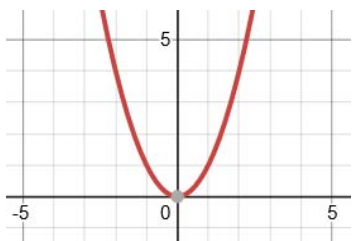
## QUADRATIC GRAPHS



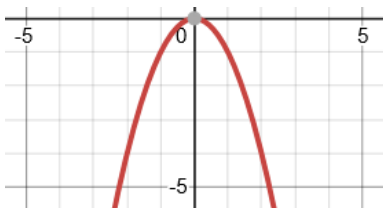
### Key Concepts

A quadratic graph will always be in the shape of a parabola.

$$y = x^2$$



$$y = -x^2$$



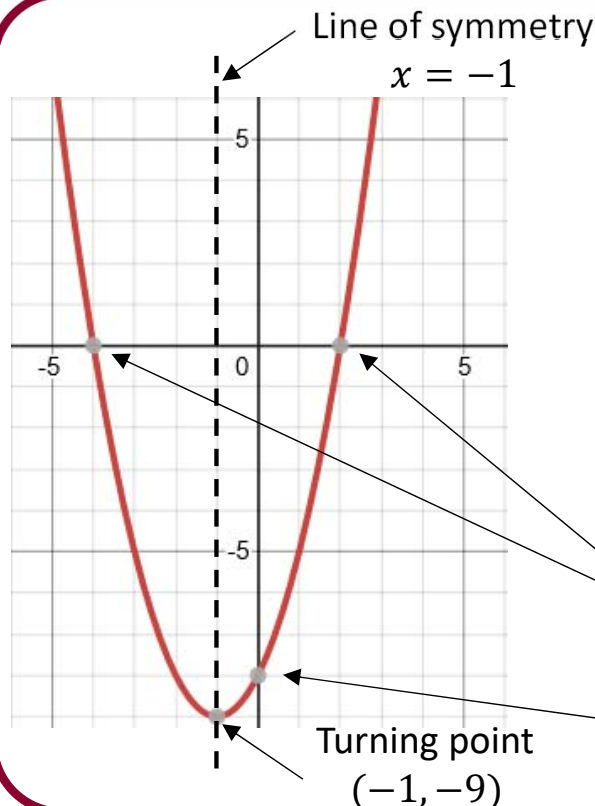
The roots of a quadratic graph are where the graph crosses the  $x$  axis. The roots are the solutions to the equation.

### Examples

$$y = x^2 + 2x - 8$$

A quadratic equation can be solved from its graph.

The roots of the graph tell us the possible solutions for the equation. There can be 1 root, 2 roots or no roots for a quadratic equation. This is dependant on how many times the graph crosses the  $x$  axis.



Roots  $x = -4$   
 $x = 2$

$y$  intercept =  $-8$

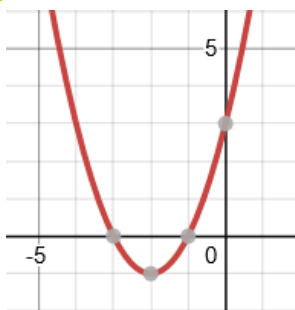
Turning point  
 $(-1, -9)$

# Y9

## Foundation

### Key Words

Quadratic  
Roots  
Intercept  
Turning point  
Line of symmetry



Identify from the graph of  $y = x^2 + 4x + 3$ :

- 1) The line of symmetry
- 2) The turning point
- 3) The  $y$  intercept
- 4) The two roots of the equation



# Maths Knowledge Organiser

## CUBIC GRAPHS



### Key Concepts

A cubic graph will always be in the shape of a parabola.

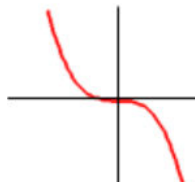
$$y = x^3$$

$a > 0$



$$y = -x^3$$

$a < 0$



The equation is of the form  $y = ax^3 + k$ , where  **$k$  is an number**.

If  $a > 0$ , the curve is **increasing**.

If  $a < 0$ , the curve is **decreasing**.

### Examples

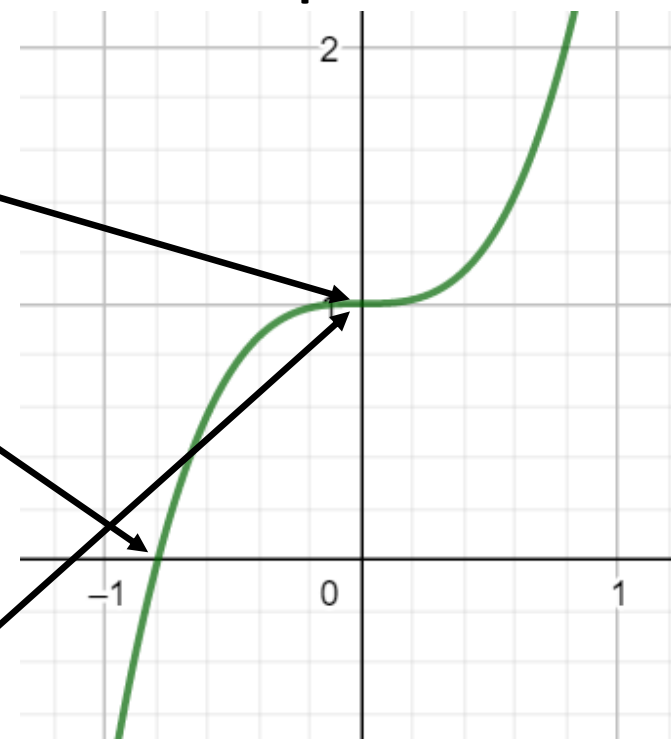
$$y = 2x^3 + 1$$

y intercept = 1

root = -0.8

*Increasing function*

*Point of inflection = (0, 1)*

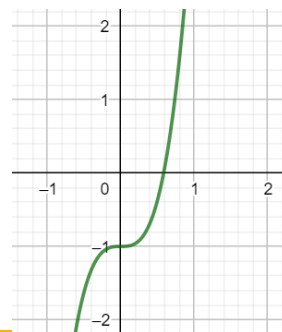


Y9

Foundation

### Key Words

Cubic  
Roots  
Intercept  
Inflection  
Extrema



Identify from the graph of  $y = 5x^3 - 1$ :

- 1) Is it increasing or decreasing?
- 2) The root of the equation
- 3) The y intercept
- 4) The point of inflection

ANSWERS 1) increasing 2) 0.6 3) -1 4) (0, -1)



# Maths Knowledge Organiser



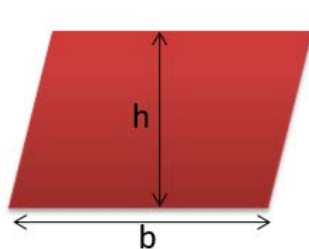
## AREA AND PERIMETER OF BASIC SHAPES

### Key Concepts

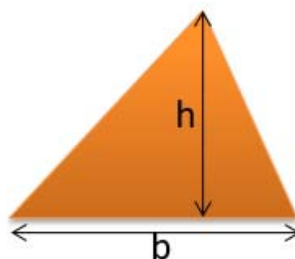
The **area** of a 2D shape is the space inside it. It is measured in units squared e.g.  $\text{cm}^2$

The **perimeter** of a shape is the distance around the edge of the shape. Units of length are used to measure perimeter e.g. mm, cm, m

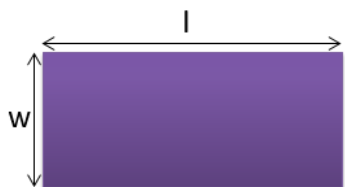
A **compound shape** is a shape made up of others joined together.



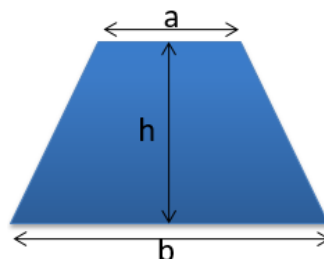
$$A = b \times h$$



$$A = \frac{b \times h}{2}$$

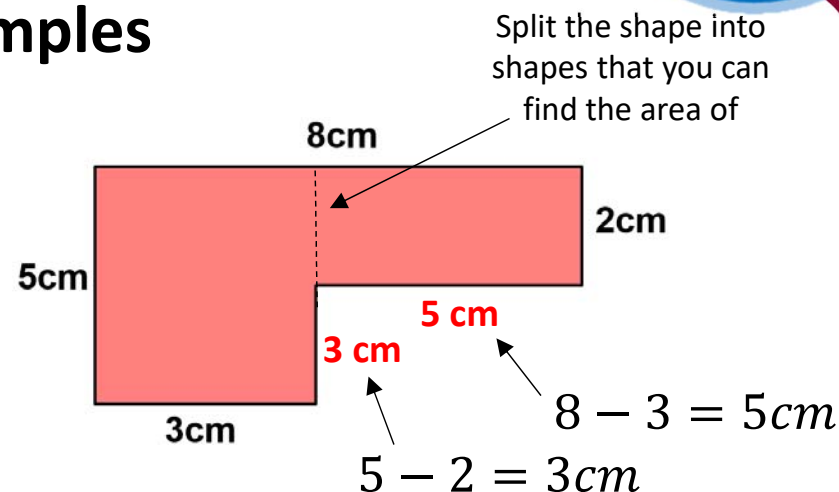


$$A = l \times w$$



$$A = \frac{(a + b) \times h}{2}$$

### Examples



$$\begin{aligned} \text{Area} &= (5 \times 3) + (2 \times 5) \\ &= 25\text{cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Perimeter} &= 3 + 5 + 8 + 2 + 5 + 3 \\ &= 26\text{cm} \end{aligned}$$

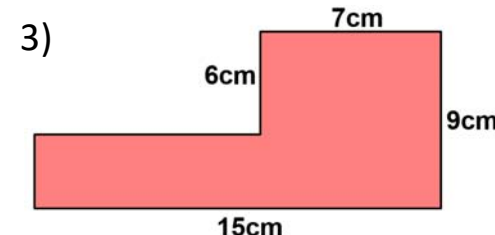
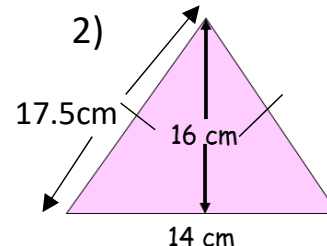
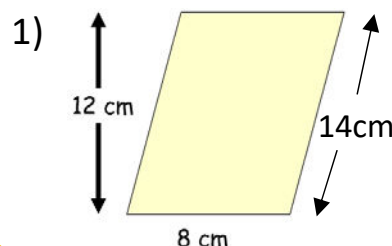
Y9

Foundation

### Key words

Area  
Perimeter  
Base  
Height  
Width  
Length

Calculate the area and perimeter of each shape:



ANSWERS: 1)  $A = 96\text{cm}^2$   $P = 44\text{cm}$  2)  $A = 112\text{cm}^2$   $P = 49\text{cm}$  3)  $A = 87\text{cm}^2$   $P = 48\text{cm}$





# Maths Knowledge Organiser



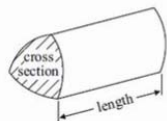
## VOLUME AND SURFACE AREA OF PRISMS

### Key Concept

The **volume** of an object is the amount of space that it occupies. It is measured in units cubed e.g.  $\text{cm}^3$ .

To calculate the volume of any prism we use:

*area of cross section*  $\times$  *length*

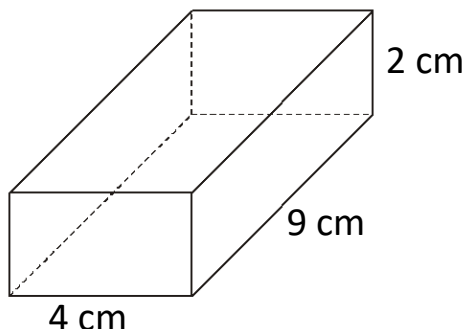


A **prism** is a 3D shape which has a continuous cross-section.

The **surface area** of an object is the sum of the area of all of its faces. It is measured in units squared e.g.  $\text{cm}^2$ .

### Examples

$$\begin{aligned}\text{Volume} &= 4 \times 9 \times 2 \\ &= 72\text{cm}^3\end{aligned}$$



**Surface area:**

$$\text{Front} = 4 \times 2 = 8$$

$$\text{Back} = 4 \times 2 = 8$$

$$\text{Side 1} = 9 \times 2 = 18$$

$$\text{Side 2} = 9 \times 2 = 18$$

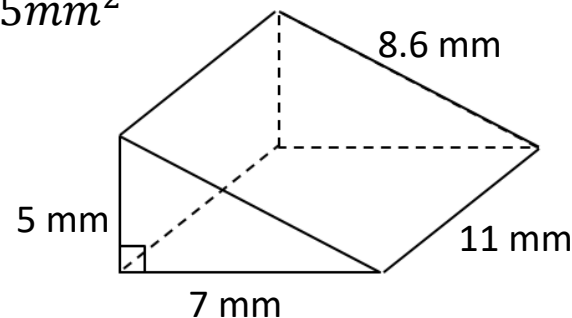
$$\text{Bottom} = 4 \times 9 = 36$$

$$\text{Top} = 4 \times 9 = 36$$

$$\text{Total} = 124\text{cm}^2$$

$$\begin{aligned}\text{Area of triangle} &= \frac{5 \times 7}{2} \\ &= 17.5\text{mm}^2\end{aligned}$$

$$\begin{aligned}\text{Volume} &= 17.5 \times 11 \\ &= 192.5\text{mm}^3\end{aligned}$$



**Surface area:**

$$\text{Front} = \frac{7 \times 5}{2} = 17.5$$

$$\text{Back} = \frac{7 \times 5}{2} = 17.5$$

$$\text{Side} = 5 \times 11 = 55$$

$$\text{Bottom} = 7 \times 11 = 77$$

$$\text{Top} = 11 \times 8.6 = 94.6$$

$$\text{Total} = 261.6\text{cm}^2$$

Y9

Foundation

### Key Words

Volume

Capacity

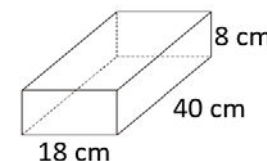
Prism

Surface area

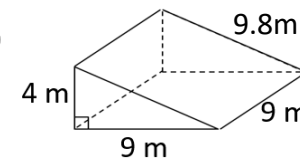
Face

Find the volume and surface area of each of these prisms:

1)



2)



ANSWERS: 1) Volume = 5760  $\text{cm}^3$  Surface area = 2368  $\text{cm}^2$  2) Volume = 162  $\text{m}^3$  Surface area = 241.2  $\text{m}^2$



# Maths Knowledge Organiser

## PERIMETER AND CIRCUMFERENCE

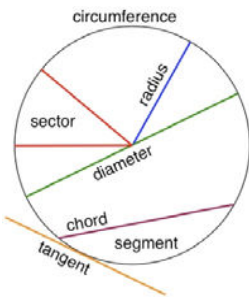


### Key Concepts

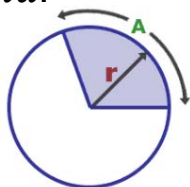
#### Parts of a circle

#### Circumference

of a circle is calculated by  $\pi d$  and is the distance around the circle.



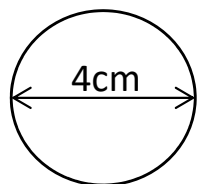
**Arc length** of a sector is calculated by  $\frac{\theta}{360} \pi d$ .



### Examples

Calculate:

#### a) Circumference

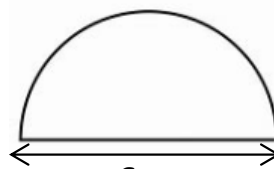


$$C = \pi \times 4 \\ = 4\pi \\ \text{or} = 12.57\text{cm}$$

#### b) Diameter when the circumference is 20cm

$$C = \pi \times d \\ 20 = \pi \times d \\ \frac{20}{\pi} = d \\ \text{Or } 6.37\text{cm}$$

#### c) Perimeter

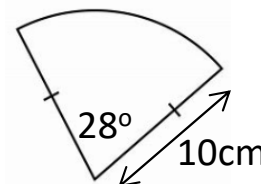


$$P = \frac{\pi \times d}{2} + d$$

$$P = \frac{\pi \times 6}{2} + 6$$

$$P = 3\pi + 6 \\ \text{Or } 15.42\text{cm}$$

#### d) Arc length



$$\text{Arc} = \frac{\theta}{360} \times \pi \times d$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 2 \times 10$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 20$$

$$\text{Arc} = \frac{14}{9} \pi \\ \text{Or } 4.89\text{cm}$$

Y9

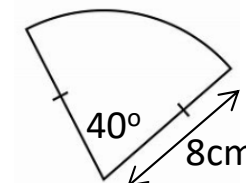
Foundation

### Key Words

Circle  
Perimeter  
Circumference  
Radius  
Diameter  
Pi  
Arc

Calculate:

- 1) The circumference of a circle with a diameter of 12cm
- 2) The diameter of a circle with a circumference of 30cm
- 3) The perimeter of a semicircle with diameter 15cm
- 4) The arc length of the diagram



ANSWERS: 1)  $12\pi$  or 37.7cm 2)  $\frac{30}{\pi}$  or 9.54cm 3) 38.56cm 4)  $\frac{9}{16}\pi$  or 5.59cm



# Maths Knowledge Organiser

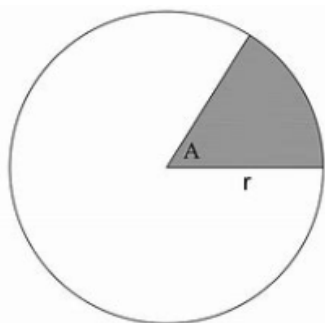
## AREA OF CIRCLES AND PART CIRCLES



### Key Concepts

The **area** of a circle is calculated by  $\pi r^2$

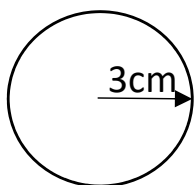
The **area of a sector** is calculated by  $\frac{\theta}{360} \pi r^2$



**Y9**  
**Foundation**

Calculate:

a) **Area**



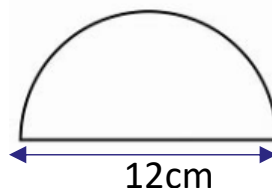
$$\begin{aligned} A &= \pi \times 3^2 \\ &= 9\pi \\ \text{or } &= 28.3\text{cm}^2 \end{aligned}$$

b) **Radius** when the area is  $20\text{cm}^2$

$$\begin{aligned} A &= \pi \times r^2 \\ 20 &= \pi \times r^2 \\ \frac{20}{\pi} &= r^2 \\ \sqrt{\frac{20}{\pi}} &= r \\ \text{Or } &2.52\text{cm} \end{aligned}$$

### Examples

c) **Area**



$$\begin{aligned} P &= \frac{\pi \times r^2}{2} \\ P &= \frac{\pi \times 6^2}{2} \\ P &= 18\pi \\ \text{Or } &56.55\text{cm}^2 \end{aligned}$$

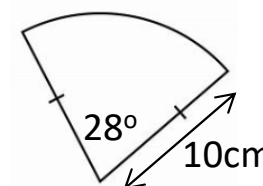
d) **Area of a sector**

$$\text{Arc} = \frac{\theta}{360} \times \pi \times r^2$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 10^2$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 100$$

$$\begin{aligned} \text{Arc} &= \frac{70}{9} \pi \\ \text{Or } &= 24.43\text{cm} \end{aligned}$$

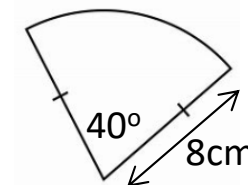


### Key Words

**Circle**  
**Area**  
**Radius**  
**Diameter**  
**Pi**  
**Sector**

Calculate:

- 1) The area of a circle with a radius of 9cm
- 2) The radius of a circle with an area of  $45\text{cm}^2$
- 3) The area of a semicircle with diameter of 16cm
- 4) The area of the sector in the diagram



ANSWERS: 1)  $81\pi$  or  $254.47\text{cm}^2$  2)  $\sqrt{\frac{45}{\pi}}$  or  $3.78\text{cm}$  3)  $32\pi$  or  $100.53\text{cm}^2$  4)  $\frac{9}{64}\pi$  or  $22.34\text{cm}^2$



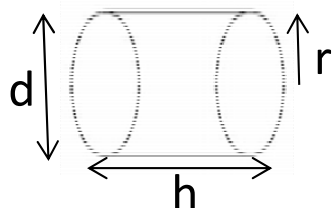
# Maths Knowledge Organiser



## VOLUME AND SURFACE AREAS OF CYLINDER

### Key Concepts

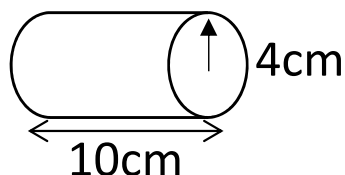
A **cylinder** is a **prism** with the cross section of a circle.



The **volume** of a cylinder is calculated by  $\pi r^2 h$  and is the space inside the 3D shape

The **surface area** of a cylinder is calculated by  $2\pi r^2 + \pi dh$  and is the total of the areas of all the faces on the shape.

From the diagram calculate:



a) **Volume**

$$V = \pi \times r^2 \times h$$

$$V = \pi \times 4^2 \times 10$$

$$V = 160\pi$$

$$\text{Or} = 502.65\text{cm}^3$$

### Examples

b) **Surface Area** – You can use the net of the shape to help you

*Area of two circles*

$$= 2 \times \pi \times r^2$$

$$= 2 \times \pi \times 4^2$$

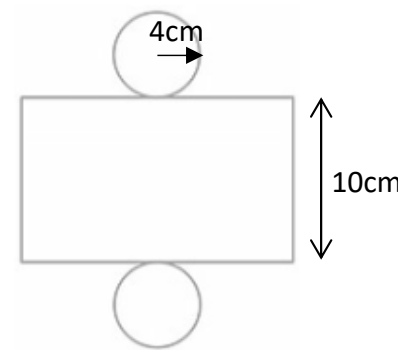
$$= 32\pi$$

*Area of rectangle*

$$= \pi \times d \times h$$

$$= \pi \times 8 \times 10$$

$$= 80\pi$$



$$\text{Surface Area} = 32\pi + 80\pi$$

$$= 112\pi$$

$$\text{or} = 351.86\text{cm}^3$$

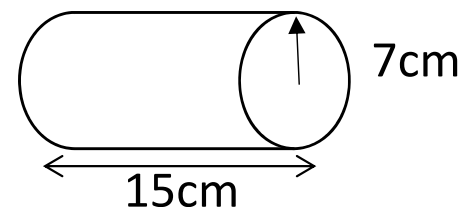
Y9

Foundation

### Key Words

Cylinder  
Surface Area  
Radius  
Diameter  
Pi  
Volume  
Prism

Calculate the volume and surface area of this cylinder







# Maths Knowledge Organiser



## BOUNDARIES

### Key Concepts

The boundaries of a number derive from **rounding**.

E.g. State the boundaries of 360 when it has been rounded to 2 significant figures:

$$355 \leq x < 365$$

E.g. State the boundaries of 4.5 when it has been rounded to 2 decimal place:

$$4.45 \leq x < 4.55$$

These boundaries can also be called the **error interval** of a number.

	+	-	$\times$	$\div$
Upper bound answer	$UB_1 + UB_2$	$UB_1 - LB_2$	$UB_1 \times UB_2$	$UB_1 \div LB_2$
Lower bound answer	$LB_1 + LB_2$	$LB_1 - UB_2$	$LB_1 \times LB_2$	$LB_1 \div UB_2$

A restaurant provides a cuboid stick of butter to each table. The dimensions are 30mm by 30mm by 80mm, correct to the nearest 5mm. Calculate the upper and lower bounds of the volume of the butter.

$$Volume = l \times w \times h$$

$$Upper\ bound = 32.5 \times 82.5 \times 32.5 = 87140.63mm^3$$

$$Lower\ bound = 27.5 \times 77.5 \times 27.5 = 58609.38mm^3$$

### Examples

When completing calculations involving boundaries we are aiming to find the greatest or smallest answer.

$$D = \frac{x}{y}$$

$x = 99.7$  correct to 1 decimal place.  
 $y = 67$  correct to 2 significant figures.  
Work out an upper and lower bounds for  $D$ .

$$Upper\ bound\ D = \frac{99.75}{66.5} = 1.5$$

$$Lower\ bound\ D = \frac{99.65}{67.5} = 1.48$$

Y9

Foundation

Key Words

Bound  
Upper  
Lower

Accuracy  
Rounding

- 1) Jada has 100 litres of oil, correct to the nearest litre. The oil is poured into tins of volume 1.5 litres, correct to one decimal place. Calculate the upper and lower bounds for the number of tins that can be filled.
- 2) There are 110 identical marbles in a bag. A marble is taken and weighed as 15.6 g to the nearest tenth of a gram. Find the upper and lower bounds for the weight of all the marbles.

ANSWERS: 1)  $LB = 69.3 \approx 69$   $UB = 69.3 \approx 69$   $UB = 64.2 \approx 64$  2)  $LB = 1710.5\text{ g}$   $UB = 1721.5\text{ g}$